

Electromagnetic Processes in Three-Nucleon Systems

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Results gained for electron scattering on ^3He in a nonrelativistic framework are reviewed. The electromagnetic current is truncated to a single nucleon operator, but the interaction among the three nucleons is treated exactly. Thus initial and final 3N states are evaluated consistently as solutions of Faddeev equations based on realistic NN forces. The correct inclusion of the final state interaction turned out to be important. The agreement to data is reasonably good, but the neglect of MEC's can be seen. That inconsistency should be removed. For pd capture processes we included some MEC's via the Siegert theorem, which dramatically improves the description of the pd capture data.

1 Introduction

Elastic and inelastic electron scattering on $^3\text{He}(^3\text{H})$ as well as photodisintegration of ^3He or pd capture have been studied since many years¹. One hopes to get insights into the 3N bound state wavefunctions and into the hadronic current operator. The single nucleon momentum distribution, NN correlation functions and d-state admixtures are prominent examples of 3N bound state properties; electromagnetic form factors of the hadrons (especially the ones of the neutron), the role and properties of two-nucleon currents or even three-nucleon currents and their consistency to the underlying nuclear forces are important issues related to the current operator. Last not least for higher energy and momentum transfers brought in by the photon into the nuclear system relativistic effects can no longer be neglected and call for strong efforts to widen the familiar nonrelativistic Schrödinger equation into the realm of

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relativity. Only in relation to a relativistic formulation of an effective hadronic theory will it be possible to control the transition region from hadronic to quark degrees of freedom.

The contribution of this article will cover only a small section of this wide arena: the nonrelativistic regime and a still truncated current operator. But the results are promising and will serve as benchmarks. A very important ingredient is the exact treatment of the interaction among the three nucleons in continuum states, whether it is the final state interaction in electron or photon induced breakup processes of ^3He or the initial state interaction in pd capture processes. This is described in section II in two examples and we refer to ² for more detailed presentations. Needless to say that the three-nucleon wavefunctions should be based on realistic nuclear forces. We then cover in section III many applications in the field of electron scattering on ^3He (^3H). They are all based on the most simple nonrelativistic single nucleon current operator. It is only in section IV that we take into account some mesonic exchange currents via Siegert's theorem³. As we shall see their effects on the tensor polarization in a pd capture process are very strong. We conclude in section V.

2 The Exact Treatment of FSI

Once the photon is absorbed by the hadronic 3N system the three nucleons are no longer bound and scatter among each other. This is exemplified for the process $^3\text{He}(e,e'p)d$ and based on a single nucleon current operator in Fig 1.

The nuclear matrixelement

$$N^\mu \equiv \langle \Psi_{pd}^{(-)} | j^\mu(Q) | \Psi_{^3\text{He}} \rangle \quad (1)$$

is expanded into a multiple scattering series in powers of the NN t-matrices acting among the three final nucleons. Obviously $\Psi_{pd}^{(-)}$ is a 3N scattering state, $j^\mu(Q) = \sum_{i=1}^3 j_{(i)}^\mu(Q)$ the single nucleon current operator and $\Psi_{^3\text{He}}$ the 3N bound state. In the first three diagrams the final nucleon and the deuteron do not interact. We denote the first diagram as PWIA and the first three as PWIAS, where "S" stands for symmetrization of the final state. Then come six processes where the final nucleon interacts once with the constituents of the deuteron. The processes of second and third order are also indicated. This infinite series is often diverging and has therefore to be summed up into an integral equation.

We introduce the following notation : $|\phi\rangle$ is the final channel state composed of a deuteron and a free nucleon, $t_i \equiv t_{jk}$ the NN (off shell) t-matrix for

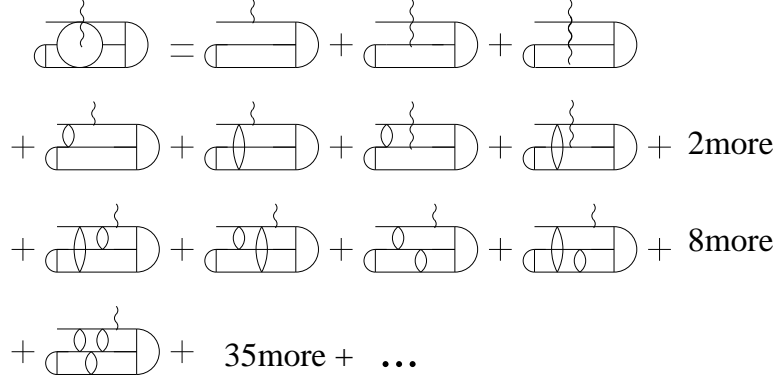


Figure 1: The multiple rescattering series for the process ${}^3\text{He}(e,e'p)d$. The larger half moon stands for the ${}^3\text{He}$ state, the wavy line for the photon, horizontal lines for freely propagating nucleons, the ovals for NN t-matrices and the small half moon for the final deuteron.

the pair jk , G_0 the free 3N propagator, j the current operator and Ψ_b the 3N bound state. Then the rescattering terms in Fig. 1 can be written as

$$N_{\text{rescatt}} \equiv \langle \phi | t_3 G_0 j | \Psi_b \rangle + \langle \phi | t_2 G_0 j | \Psi_b \rangle + \langle \phi | (t_2 G_0 t_3 G_0 + t_3 G_0 t_2 G_0 + t_3 G_0 t_1 G_0 + t_2 G_0 t_1 G_0) j | \Psi_b \rangle + \dots (2)$$

This can be formulated concisely with the help of an operator $P \equiv P_{12}P_{23} + P_{13}P_{23}$, which is the sum of a cyclical and an anticyclical permutation:

$$\begin{aligned} N_{\text{rescatt}} &= \langle \phi | P t_1 G_0 j | \Psi_b \rangle + \langle \phi | P t_1 G_0 P t_1 G_0 j | \Psi_b \rangle + \dots \\ &= \langle \phi | P \{ t_1 G_0 j | \Psi \rangle + (t_1 G_0 P) t_1 G_0 j | \Psi_b \rangle \\ &\quad + (t_1 G_0 P)(t_1 G_0 P) t_1 G_0 j | \Psi \rangle + \dots \rangle \\ &\equiv \langle \phi | P | U \rangle \end{aligned} \quad (3)$$

It follows that the quantity $|U\rangle$

$$|U\rangle \equiv t G_0 j | \Psi_b \rangle + (t G_0 P) t G_0 j | \Psi_b \rangle + (t G_0 P)(t G_0 P) t G_0 j | \Psi_b \rangle + \dots \quad (4)$$

obeys the integral equation

$$|U\rangle = t G_0 j | \Psi_b \rangle + t G_0 P | U \rangle \quad (5)$$

which is of the Faddeev-type. The inhomogeneous term is driven by the NN t-matrix (we dropped the index 1), the current operator and the target bound state. This integral equation can be solved exactly for any type of realistic NN

force². The nuclear matrixelement then takes the form (up to a symmetrization factor of 3)

$$N^\mu = \langle \phi | j | \Psi_b \rangle + \langle \phi | P | U \rangle \quad (6)$$

As a second example for treating FSI processes exactly we regard inclusive scattering, where response function to some operator \hat{O} occur:

$$R \equiv \sum_f |\langle f | \hat{O} | i \rangle|^2 \delta(\omega + E_i - E_f) \quad (7)$$

Here E_i and E_f are exact energy eigenvalues of the Hamiltonian H to the initial and final states $|i\rangle$ and $|f\rangle$ and ω the energy carried by the photon. Apparently one can rewrite R as

$$\begin{aligned} R &= -\frac{1}{\pi} \text{Im} \sum_f \langle i | \hat{O}^\dagger | f \rangle \frac{1}{\omega + E_i - E_f + i\epsilon} \langle f | \hat{O} | i \rangle \\ &= -\frac{1}{\pi} \text{Im} \langle i | \hat{O}^\dagger \frac{1}{\omega + E_i - H + i\epsilon} \hat{O} | i \rangle \end{aligned} \quad (8)$$

using the completeness relation. Standard steps^{2,4} applied to the 3N problem $(\omega + E_i - E_f + i\epsilon)^{-1} \hat{O} | i \rangle$ leads to

$$R = -\frac{1}{\pi} \text{Im} \langle i | \hat{O}^\dagger (1 + P) G_0 | \tilde{U} \rangle \quad (9)$$

where $|\tilde{U}\rangle$ obeys the integral equation.

$$|\tilde{U}\rangle = (1 + tG_0) \hat{O} | i \rangle + tPG_0 |\tilde{U}\rangle \quad (10)$$

We see the same integral kernel as in (5). This result is formulated for the case $\hat{O} \equiv \sum_{i=1}^3 \hat{O}(i)$. Our algorithm to solve Eqs. (5) and (10) and the technicalities connected with the partial-wave decomposition are described in². The expressions for the observables in terms of the nuclear matrixelements can be found also in².

3 Applications

The results to be presented are based on a strictly nonrelativistic treatment and the simple single nucleon current operator:

$$\langle \vec{p}' | j^0 | \vec{p} \rangle = F_1^n (\vec{p}' - \vec{p}) \Pi^n + F_1^p (\vec{p}' - \vec{p}) \Pi^p$$

$$\begin{aligned}
\langle \vec{p}' | j | \vec{p} \rangle &= \frac{\vec{p}' + \vec{p}}{2m} \{ F_1^n(\vec{p}' - \vec{p}) \Pi^n + F_1^p(\vec{p}' - \vec{p}) \Pi^p \} \\
&+ \frac{i\sigma \times (\vec{p}' - \vec{p})}{2m} \{ (F_1^n(\vec{p}' - \vec{p}) + 2mF_2^n(\vec{p}' - \vec{p})) \Pi^n \\
&+ (F_1^p(\vec{p}' - \vec{p}) + 2mF_2^p(\vec{p}' - \vec{p})) \Pi^p \}
\end{aligned} \tag{11}$$

Here $F_{1,2}$ are the electromagnetic nucleon form factors and $\Pi^{n,p}$ are neutron and proton projection operators.

3.1 Elastic scattering

This is an old topic⁵ and our results based on the current given in Eq. (11) can be found in⁶. Throughout this overview we restrict ourselves to three momentum transfers of the photon $|\vec{Q}| \leq 400 \text{ MeV/c}$, where relativity is expected to play still a minor role. Within that limited interval the charge form factor is reasonably well described. For the magnetic form factor discrepancies develop towards the larger $|\vec{Q}|$ values, which are known to be cured by the action of mesonic exchange currents⁷.

3.2 Inclusive Scattering

From the experience in elastic scattering one has to expect that the longitudinal structure function R_L should be fairly well predicted and deficiencies should show up in R_T due to the missing MEC's. This is indeed the outcome² as shown in Figs. 2 and 3 for $|\vec{Q}| = 174, 250$ and 300 MeV/c .

The treatment of FSI is crucial as is drastically demonstrated in Fig. 4.

In Fig. 5 the two structure functions are displayed based on rescattering included up to different orders in the NN t-matrix. It is interesting to see that it diverges for lower ω 's for R_L and that R_T is very well described truncating the series (erroneously) at first order in t .

We would like to add some results² on the extraction of the pp correlation function from the Coulomb sum. We show in Fig. 6 the pp correlation functions in ^3He for point and extended proton:

$$C_{point}^{pp}(x) = \frac{1}{2} \sum_M \langle \Psi_b M | \sum_{i \neq j} \Pi^p(i) \Pi^p(j) \delta(\vec{x} - (\vec{r}_i - \vec{r}_j)) | \Psi_b M \rangle \tag{12}$$

$$C_{ext}^{pp}(x) = \frac{1}{2} \sum_M \int d\vec{r} \langle \Psi_b M | \sum_{i \neq j} \Pi^p(i) \Pi^p(j) F_1^p(\vec{r} + \vec{x} - \vec{r}_i) F_1^p(\vec{r} - \vec{r}_j) | \Psi_b M \rangle \tag{13}$$

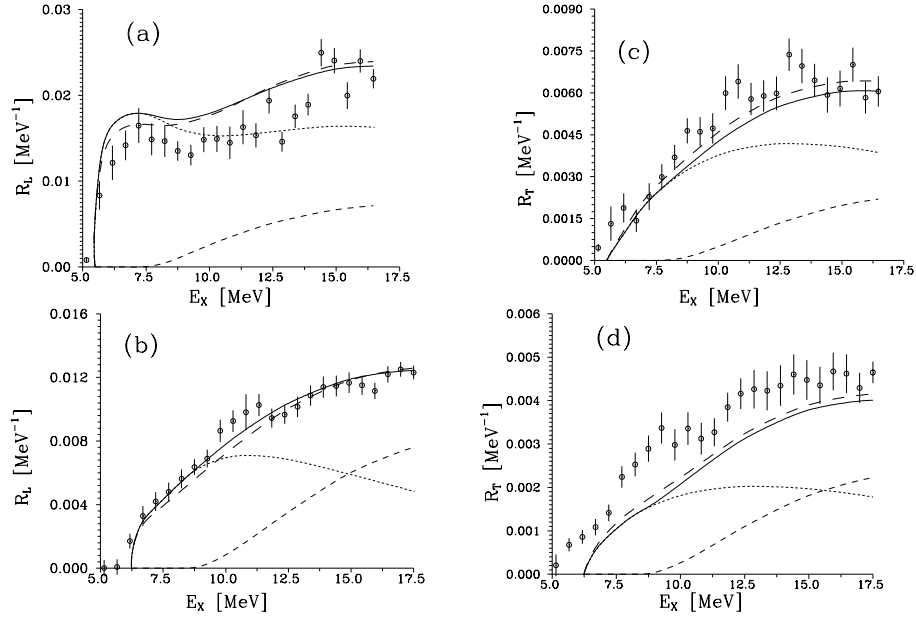


Figure 2: (a) ^3He longitudinal, (b) ^3H longitudinal, (c) ^3He transversal and (d) ^3H transversal response functions at $Q = 174\text{MeV}/c$. Comparison of data⁸ to Bonn B^{25} (solid line) and MT I-II P^6 (long dashed line) calculations. Short dashed and medium long dashed lines are the separate contributions for the Nd and 3N breakups.

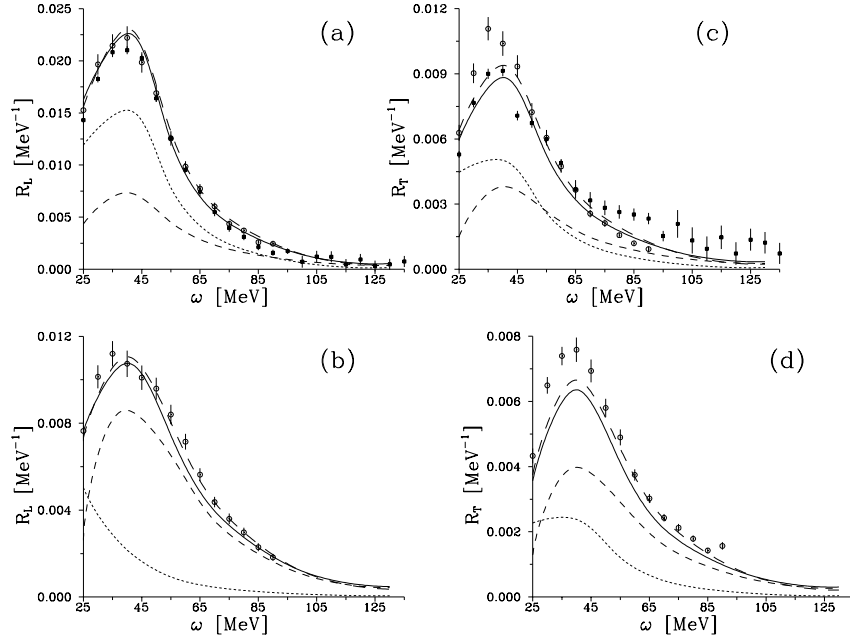


Figure 3: Same as in Fig. 2 for $Q=250\text{MeV}/c$. Data (circles) from⁹ and (squares) from¹⁰.

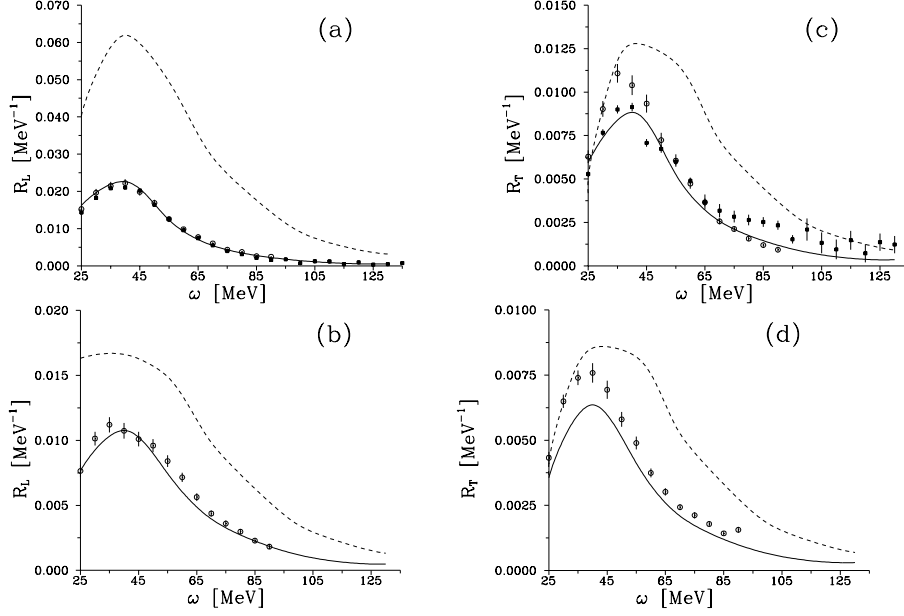


Figure 4: (a) ^3He longitudinal, (b) ^3H longitudinal, (c) ^3He transversal and (d) ^3H transversal response functions at $Q=250\text{MeV}/c$. The PWIAS predictions (short dashed) are compared to the full Bonn B calculation and the data.

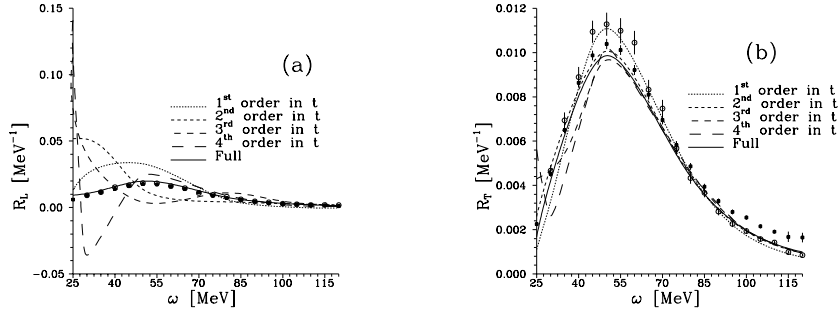


Figure 5: The two responses for ^3He , (a) longitudinal and (b) transversal at $Q=300\text{MeV}/c$. Shown are the PWIAS plus different orders of rescattering in the two-nucleon t -matrix. No Padé has been used. *Full* and data as in Fig. 3.

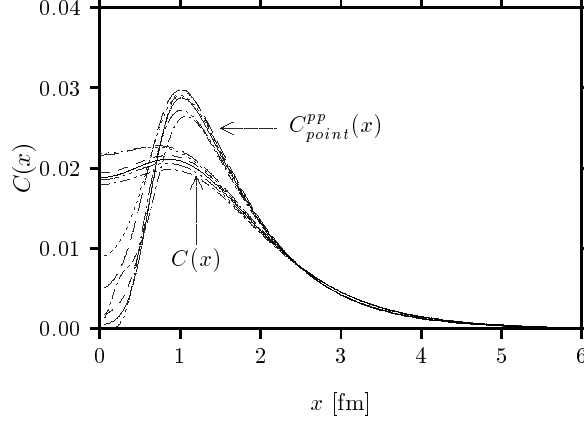


Figure 6: The two-nucleon correlation function $C(x)$ of Eq.(13) and the point proton-proton correlation function of Eq. (12) for various NN forces: AV18²⁷ (solid), Bonn B²⁵ (dashed), Nijmegen93²⁸ (short dashed), Nijmegen P²⁸ (dotted), Paris²⁹ (dash-dotted) and Ruhrpot³⁰ (dash-double-dotted).

with

$$F_1^p(\vec{r}) = \frac{1}{(2\pi)^3} \int d\vec{Q} e^{-i\vec{Q}\vec{r}} F_1^p(\vec{Q}) \quad (14)$$

We see a spread for different underlying NN potentials caused by their different short range repulsions. The nucleonic form factors fill the dip at short distances. These configuration space features are reflected again in a spread in the correlation function in momentum space (see Fig. 7), which is defined as

$$C(|\vec{Q}|) = \int d\vec{x} e^{i\vec{Q}\vec{x}} C_{ext}^{pp}(\vec{x}) \quad (15)$$

It has been known for long time¹³ that the Coulomb sum is related to $C(|\vec{Q}|)$. If we define

$$S_L(|\vec{Q}|) \equiv \frac{1}{Z} \int_{\omega_{min}}^{\infty} d\omega R_L(\omega, |\vec{Q}|) \quad (16)$$

then under the assumption of a single nucleon density operator one finds (neglecting the neutron contribution)

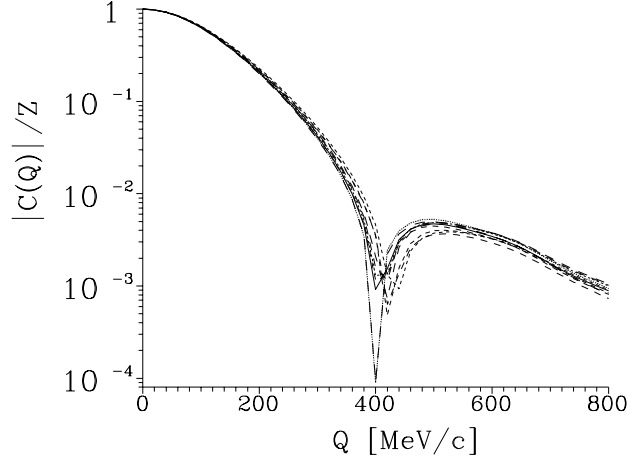


Figure 7: The two-nucleon correlation function $|C(Q)|/Z$ of Eq. (15) for various NN forces. Description as in Fig. 6.

$$\frac{1}{Z}C(|\vec{Q}|) = S_L(|\vec{Q}|) - \{F_1^p(\vec{Q})\}^2 + ZF_{ch}^2(\vec{Q}) \quad (17)$$

where F_{ch} is the charge form factor for elastic electron - ^3He scattering. All four quantities entering Eq.(17) are displayed in Fig. 8. One sees the strong cancellation on the right hand side and the resulting $C(|\vec{Q}|)$ is roughly an order of magnitude smaller than F_1^p . Apparently the control of C will pose a challenge to experiment and theory. Our simple theory for the left hand side of Eq. (15) fails in comparison to the experimental values inserted into the right hand side, as seen in Fig. 9.

It has been shown in ¹⁴ that relativistic corrections in the current operator and two-body current contributions remove most of the discrepancy. These effects are large in relation to C and no longer corrections. Clearly they call for a relativistic framework which might even change the interpretation and structure of the term C .

The access to S_L requires extrapolation beyond the presently available

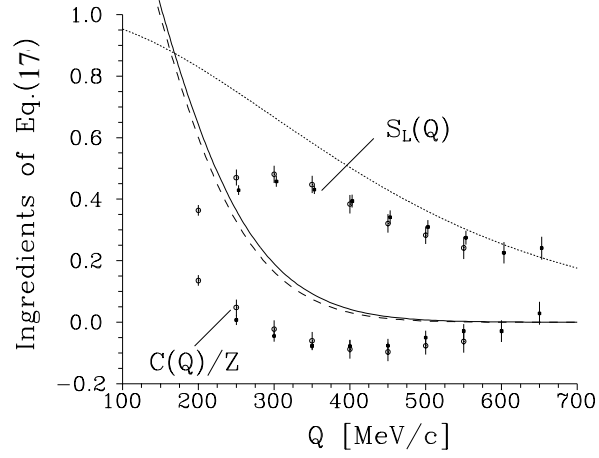


Figure 8: The ingredients of Eq. (17) for ^3He : the experimental $S_L(Q)$ (open circles⁹ and closed squares¹⁰) and $[F_1^p(Q)]^2$ from¹¹ (dotted) and $ZF_{ch}^2(Q)(1 - q_\mu^2/4M_{3He}^2)$ (experimental values¹²)(solid curve), our theoretical values (dashed curve) and $C(Q)/Z$.

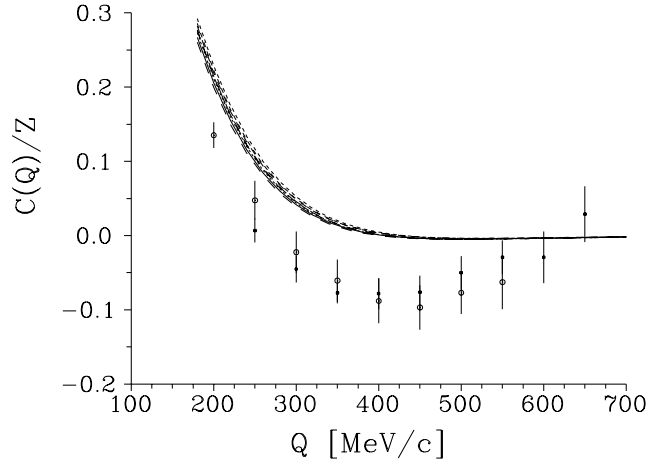


Figure 9: Theoretical proton-proton correlation functions in ^3He evaluated for various NN forces (as in Fig. 7) in comparison to the experimental correlation function $C(Q)/Z$ from Fig. 8.

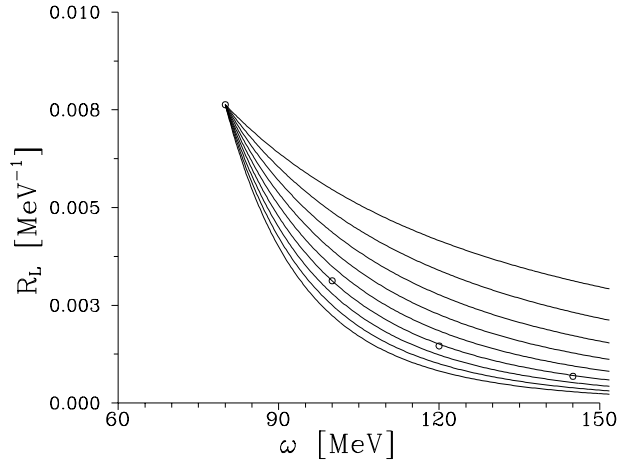


Figure 10: The extrapolation according to Eq.(18). The exponent $\alpha=4$ is favored over $\alpha=1.5, 2, 2.5, 3, 3.5, 4.5, 5, 5.5$ and 6 read from top to bottom. The open circles are theoretical values at $Q=300\text{MeV}/c$.

data points for R_L . We show in Fig. 10 that theory might help. Putting

$$R_L(\omega) = R_L(\omega_{max}) \left(\frac{\omega_{max}}{\omega} \right)^\alpha \quad (18)$$

we see that $\alpha=4$ is clearly favoured. This has been used in our analysis² and we have found that the contributions of the extrapolated tails to the Coulomb sum range between 6 and 23 % in the case of the data set⁹ and even up to 40% in case of the data¹⁰. Certainly for a future relativistic theory data less dependent on extrapolation assumptions would be desirable.

3.3 Exclusive scattering

We regard the processes ${}^3\text{He}(e,e'p)d$ and ${}^3\text{He}(e,e'd)p$, where data exist¹⁵ and new ones are coming up¹⁶. To the best of our knowledge there are not yet data which cover the proton angular distribution over the whole proton knockout peak. One example of the rather limited experimental knowledge is compared to theory in Fig. 11. The NN force (Bonn B) is kept different from zero in the states 1S_0 and 3S_1 - 3D_1 , up to total angular momentum $j_{max}=1$ and $j_{max}=2$, which clearly shows that the latter choice is sufficient. Another example over a larger range of proton scattering angles is shown in Fig. 12. In this example we see the importance of symmetrization in the final state (PWIAS) at large

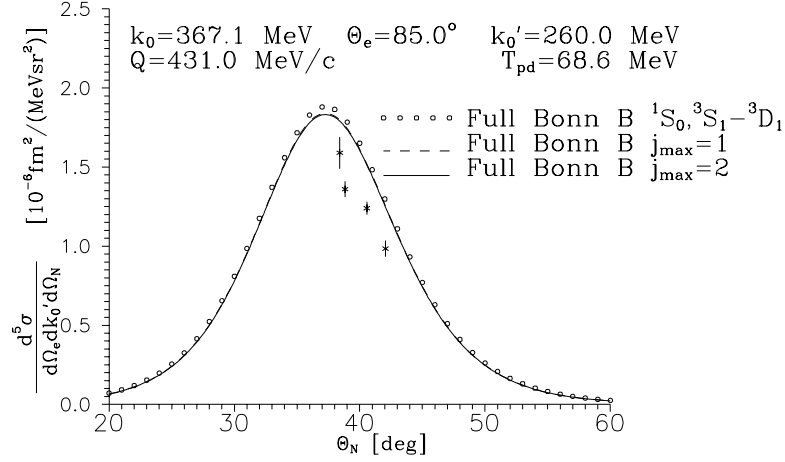


Figure 11: The quasifree proton knockout peak in pd breakup. θ_N is the proton laboratory angle. The data are from ¹⁵.

angles and of FSI for all angles. Also it is important to use a realistic NN force and higher order rescattering processes have to be summed up correctly as is demonstrated in Figs. 13 and 14. The proton angular range around 200° is where the deuteron knockout peak is located. It can be seen as a peak only by choosing the deuteron scattering angle. Unfortunately there are no data in the peak area. An example is displayed in Fig. 15. Data¹⁵ right in the deuteron peak in the so called parallel kinematics $pd \parallel \vec{Q}$ are shown in Fig. 16 in comparison to our theory. More data will come up¹⁶. That knockout of a deuteron results from a complicated series of rescattering processes as dramatically illustrated in².

3.4 Inclusive Scattering with polarized electrons and ^3He targets

The process $^3\bar{H}e(\vec{e}, e')$ has been measured^{17,18,19} with the aim to extract the magnetic form factor of the neutron. The basis for that possibility is the fact that the spin of a polarized ^3He nucleus is carried to a very large extent by a polarized neutron²⁰. The well known asymmetry expression

$$A = \frac{v_{T'} R_{T'} \cos \theta^* + v_{TL'} R_{TL'} \sin \theta^* \cos \phi^*}{v_L R_L + v_T R_T} \quad (19)$$

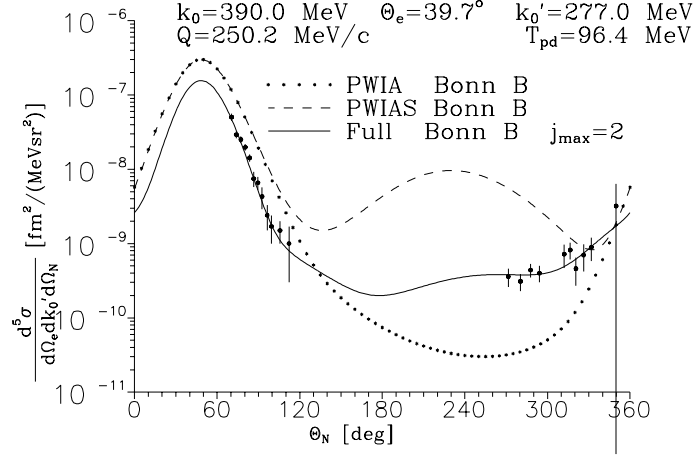


Figure 12: The full angular proton distribution of pd breakup. Comparison of PWIA, PWIAS, and the full treatment of rescattering. Data from ¹⁵.

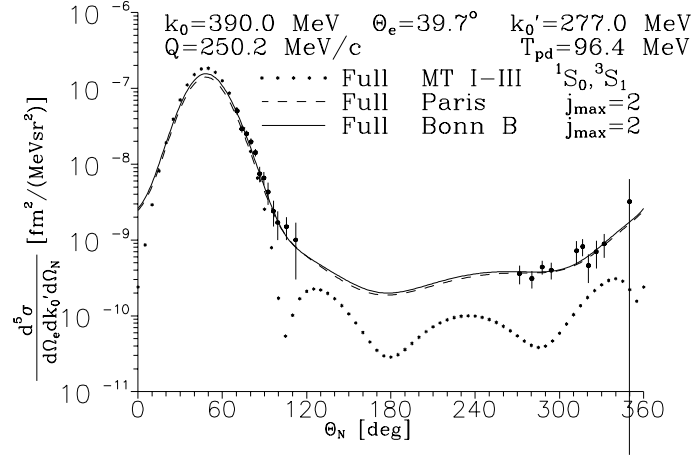


Figure 13: Comparison of Paris and Bonn B predictions to the one based on the MT I-III²⁶ NN force model.

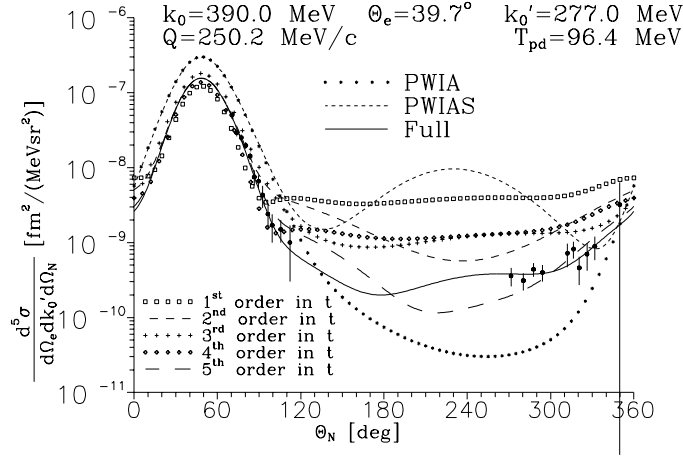


Figure 14: Comparison of PWIA, PWIAS, and partial sums of increasing orders in t -matrix added to it. The convergence toward the full solution is very slow.

expressed in terms of the angle θ^* between the direction of the ^3He spin and the photon direction reduces to $A_{T'}$ for $\theta^*=0$ and $A_{TL'}$ for $\theta^*=90$ degrees. In PWIA and reducing the ^3He state to the principle S-state (PS) one can show² that $A_{T'} \propto (G_M^{(n)})^2$ and $A_{T'L'} \propto G_E^{(n)} G_M^{(n)}$. Of course this is no longer the case if FSI is included. Nevertheless one receives information on the magnetic form factor of the neutron². We compare in Figs. 17 and 18 various approximations to our best result and to the data. The most naive picture, PWIA and PS-state approximation of ^3He fails totally for $A_{TL'}$ and is also a poor description for $A_{T'}$. Using the correct ^3He state influences $A_{TL'}$ very much but together with PWIA moves theory further away from the data. Symmetrizing the final state according to PWIAS also influences $A_{TL'}$ strongly. The partial inclusion of FSI among the two nucleons which are spectators to the photon absorption (PWIA') causes a big effect, also the additional symmetrization (PWIAS'), but it is only after inclusion of the full FSI that one approaches the data both for $A_{T'}$ and $A_{TL'}$ fairly well. More precise data for both asymmetries would be very desirable: for $A_{T'}$ to better pin down $G_M^{(n)}$ and for $A_{TL'}$ to probe 3N wave functions and the current operator.

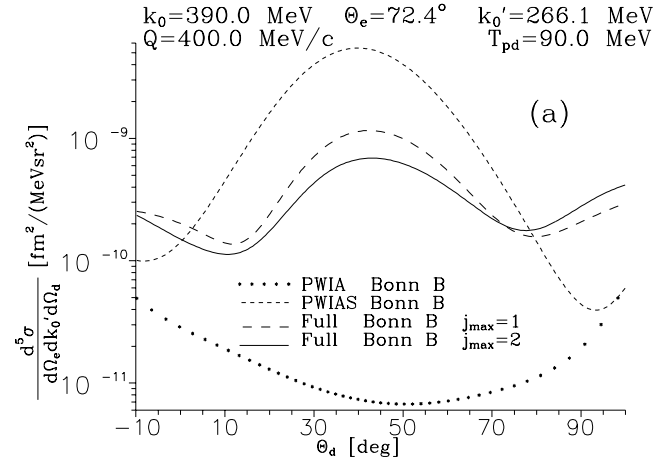


Figure 15: A deuteron knockout peak. Comparison of PWIA, PWIAS and two full calculations keeping the NN force up to $j_{\max}=1$ or 2.

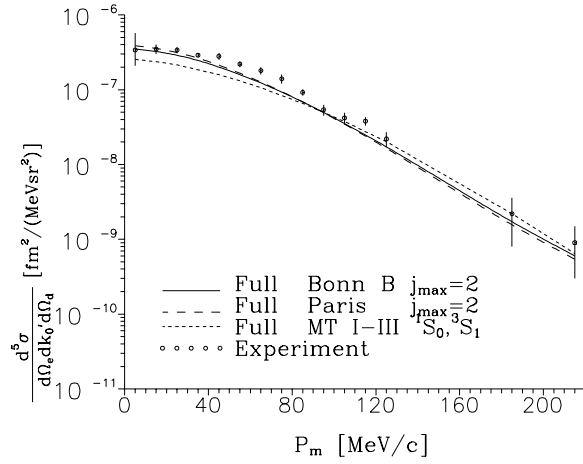


Figure 16: Data¹⁵, in parallel kinematics against missing momentum P_m are compared to the Paris²⁹, Bonn B²⁵ and MT I-II²⁶ predictions.

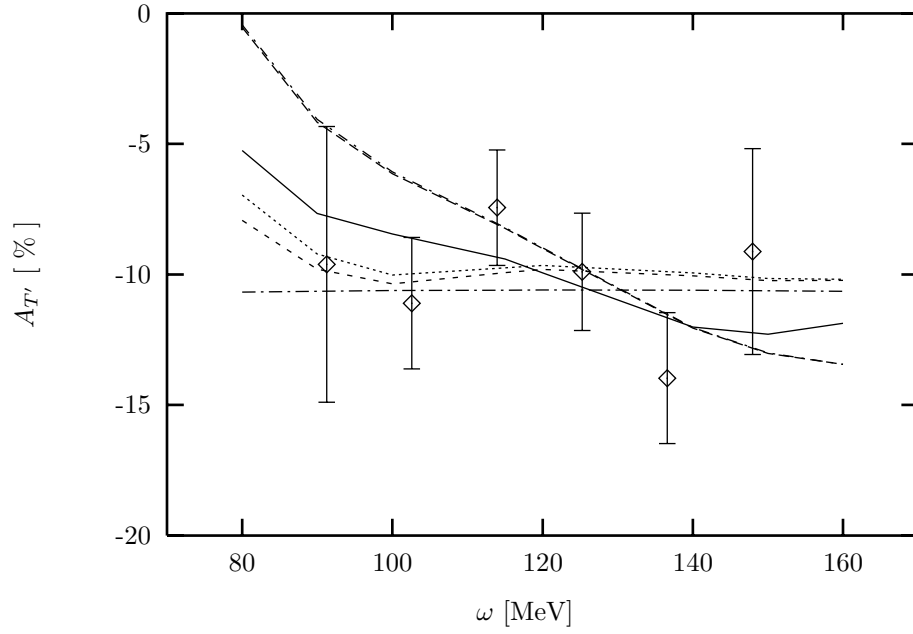


Figure 17: The transverse asymmetry $A_{T'}$ as a function of ω . The data are from Ref⁷. The six theoretical curves are PWIA(PS)(dashed-dotted), PWIA(dotted), PWIAS(short dashed), PWIA'(long dashed), PWIAS'(dashed-dotted, declined curve) and FULL (solid). Note PWIA' and PWIAS' overlap.

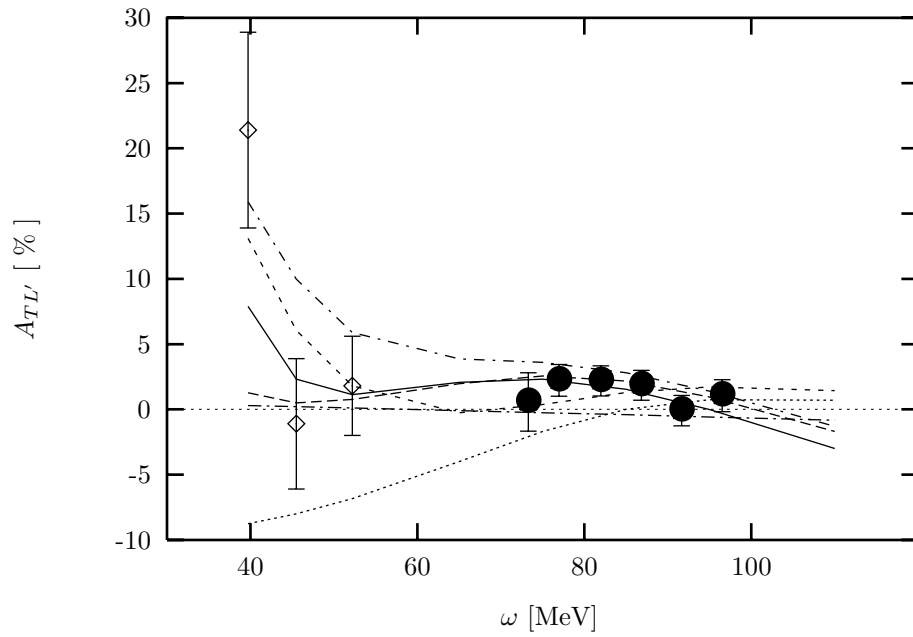


Figure 18: The transverse-longitudinal asymmetry $A_{TL'}$ as a function of ω . The data (\diamond) are from Ref⁸ and the data (\bullet) from Ref⁹. Curves as in Fig. 20. The PWIAS'-curve rises to the data point at $\omega=40$ MeV.

3.5 *pd capture*

This example shows dramatically the improvement of a theoretical description of the data if the consistency between currents and Hamiltonian is taken into account according to Siegert's idea. We show in Fig. 19 the tensor analyzing power A_{yy} for the process $\vec{d} + p \rightarrow {}^3\text{He} + \gamma$ at $E_d=45\text{MeV}$ ²¹. The data are compared to the single nucleon current prediction, which is far off and the dramatic improvement if a general current is included via the Siegert theorem in the electric multipoles. Fig. 20 demonstrates that the neglect of the initial state interaction would be a disaster. This is of course no surprise since Nd scattering at 45MeV requires the full multiple scattering series²². Fig. 21 shows the contributions of various electric multipoles and points to the correct use of Siegert's replacement of parts of the current by the density operator. No long wave length approximation is required as will be shown in a forthcoming article. Usually in the application of Siegert's theorem some terms are neglected, illustrated here by the curve " E_1 one term", whereas " $E_1, \text{both terms}$ " keeps correctly all terms. This observable A_{yy} also reacts sensitively to switching off parts of the ${}^3\text{He}$ wavefunction. Dropping the D-state related amplitudes causes A_{yy} to shift strongly away from the data as shown in Fig 22. Finally we show in Fig. 23 the pd capture cross section itself comparing in the single nucleon current approximation and using Siegerts theorem. As for A_{yy} the latter formulation is by far superior also for the cross section.

4 Conclusion

We demonstrated that the correct treatment of the 3N continuum in various electromagnetic processes in the 3N system as well as the use of realistic NN forces is very important. Though the restriction to a single nucleon current operator works often remarkably well for a convincing picture mesonic exchange currents have to be included and current conservation has to be fulfilled. For some of the observables which are accessible by other techniques this has already been achieved with promising results⁷. For exclusive processes much remains to be done. Using Siegert's idea in the pd capture process is a first step in that direction. We expect that the use of realistic forces together with a current operator consistent to them should be a sound basis to describe the data. First results shown in this small overview and restricted to small energy and momentum transfers of the photon are promising. At higher four momentum transfers relativity is required, which is a challenging task for theory.

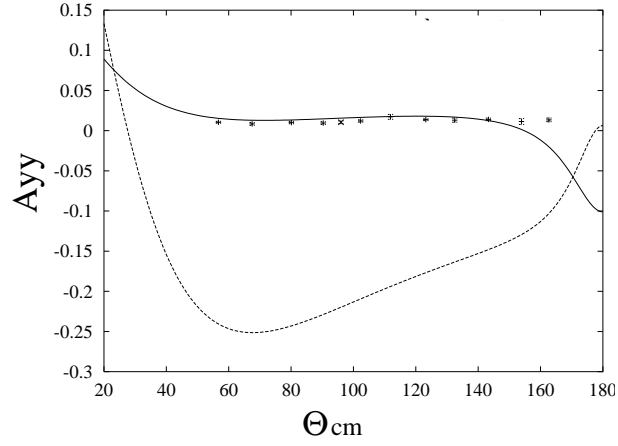


Figure 19: A_{yy} with (solid curve) and without Siegert terms (dashed curve) . Data from²¹ and the point at 96° from²³.

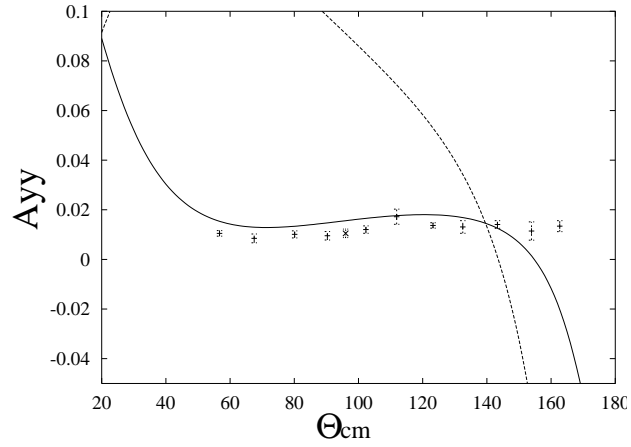


Figure 20: The importance of the initial state interaction for A_{yy} (solid curve) as compared to PWIAS (dashed curve). Data as in Fig. 19.

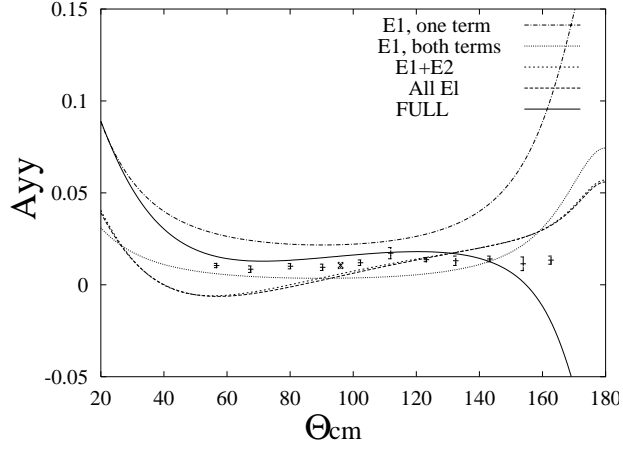


Figure 21: Various individual contributions to A_{yy} in relation to our full result. Data as in Fig. 19.

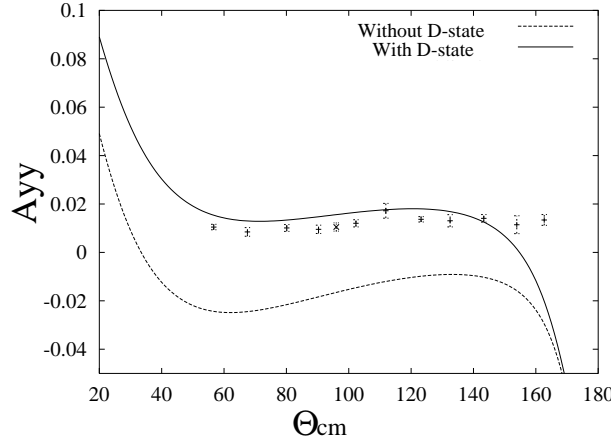


Figure 22: Effect of D-wave admixture in the ^3He bound state on A_{yy} . Data as in Fig. 19.

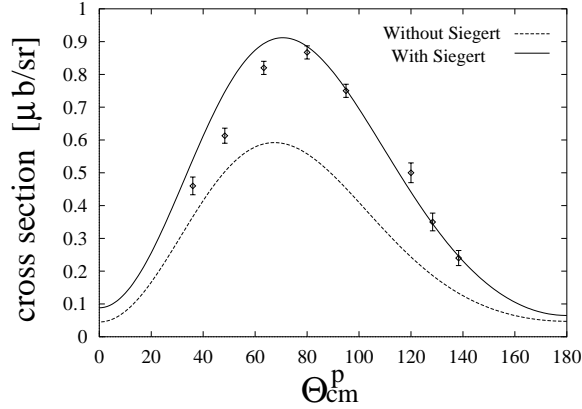


Figure 23: Cross sections for the pd capture reaction with and without Siegert terms. Data from ²⁴.

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